

# Lecture 02

## Digital Image Basics

2024-08-21

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MÉXICO

## 1. Motivation

1. Why Computer Vision for Geosciences?
2. Computer Vision processing levels

2. What is a digital image?

3. Point operations

4. Image manipulation with Python

## Computer Vision for Geosciences (CV4GS)

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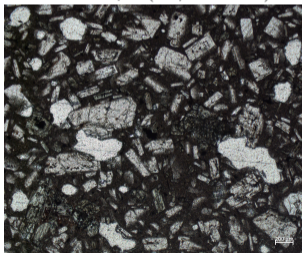
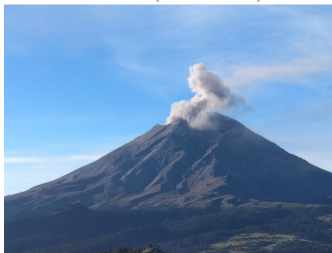
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- What is Computer Vision?

⇒ discipline focused on enabling computers to acquire, process, and interpret visual data, primarily from digital images or video

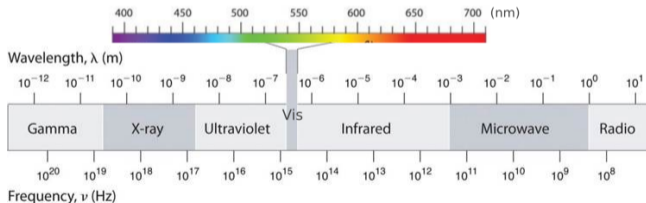
## Computer Vision for Geosciences (CV4GS)

- Sources of images for **geosciences** applications?
  - ⇒ images can be derived from different imaging techniques at different scales

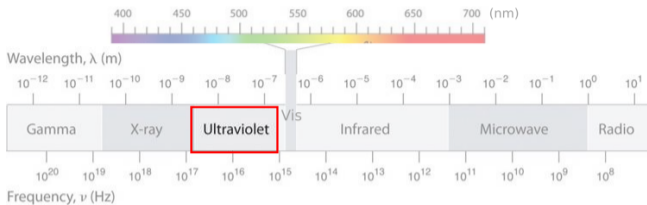
microscope ( $\sim \mu m$ -scale)camera ( $\sim m$ -scale)satellite ( $\sim km$ -scale)

## Computer Vision for Geosciences (CV4GS)

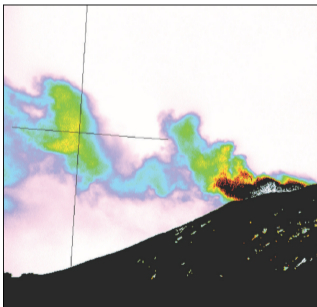
- Sources of images for geosciences applications?
  - ⇒ images can be constructed using different wavelengths spanning the entire electromagnetic spectra



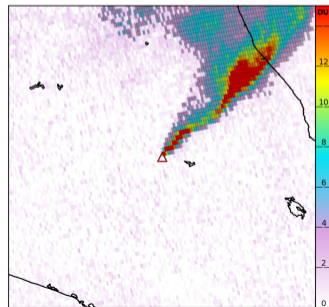
## 1.1. Why Computer Vision for Geosciences?



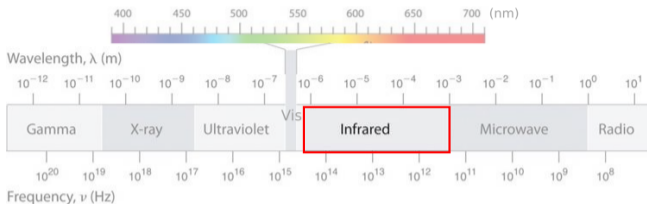
UV camera

Popocatepetl 2013-01-29 (UV camera, [Campion et al. 2018](#))

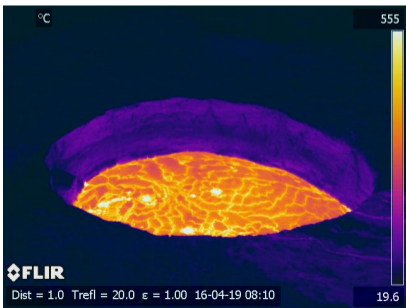
UV satellite

Popocatepetl 2019-02-17 (Sentinel-5P, [MOUNTS](#))

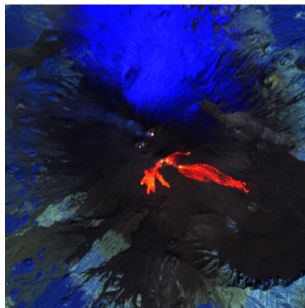
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IR camera

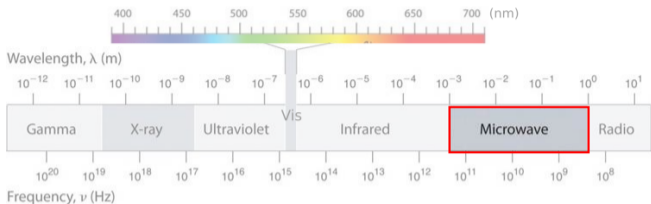
Nyiragongo 2016-04-16 (FLIR image, [Valade et al. 2018](#))

IR satellite

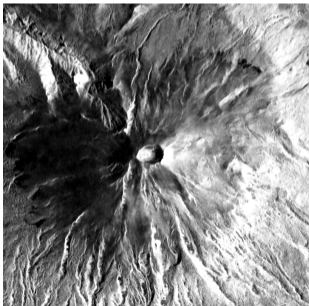
Etna 2021-02-23 (Sentinel-2 image, [MOUNTS](#))



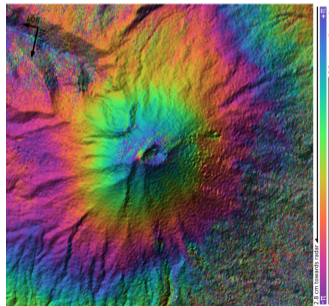
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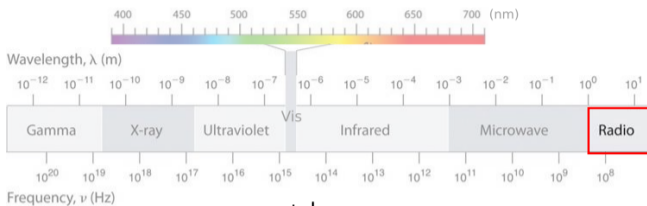
SAR satellite

Popocatepetl SAR 2021-12-25 (Sentinel-1, [MOUNTS](#))

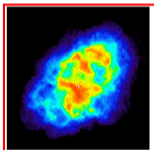
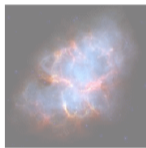
InSAR satellite

Popocatepetl InSAR interferogram 2021-12-25 dt=6 days ([MOUNTS](#))

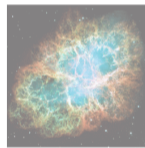
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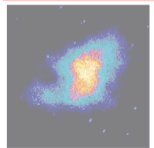
telescope

**Radio wave (VLA)**

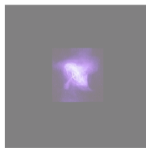
Infrared radiation (Spitzer)



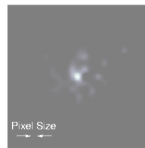
Visible light (Hubble)



Ultraviolet radiation (Astro-1)

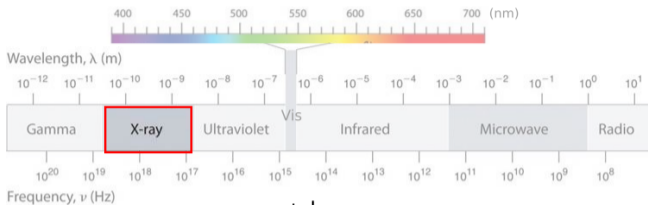


Low-energy X-ray (Chandra)

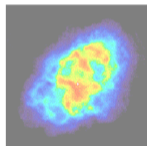
High-energy X-ray (HEFT)  
\*\*\* 15 min exposure \*\*\*

Crab Nebula - remanent of an exploded star (supernova)

## 1.1. Why Computer Vision for Geosciences?



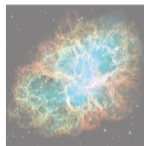
telescope



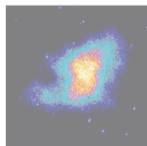
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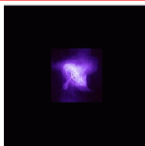
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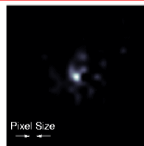
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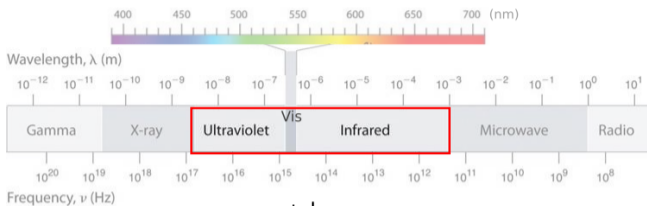


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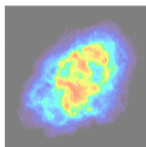
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telescope



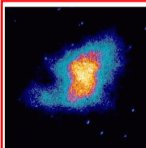
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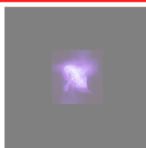
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Visible light (Hubble)



Ultraviolet radiation (Astro-1)



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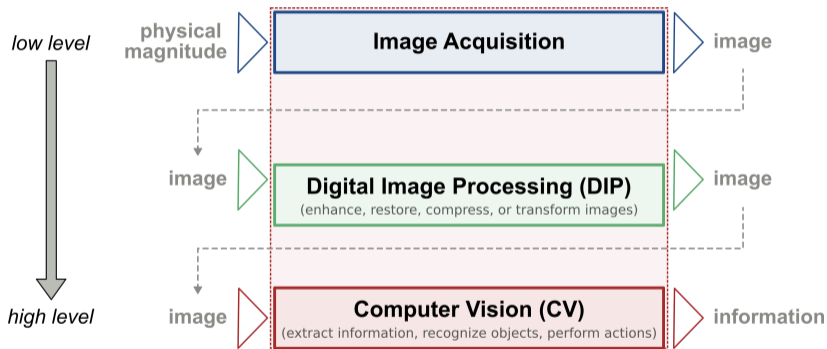
High-energy X-ray (HEFT)

Pixel Size

\*\*\* 15 min exposure \*\*\*

Crab Nebula - remnant of an exploded star (supernova)

## From image acquisition to image processing:



*“Computer Vision tasks include methods for **acquiring**, **processing**, **analyzing** and understanding digital images, and extraction of high-dimensional data from the real world in order to produce numerical or symbolic information, e.g., in the forms of decisions”.*

## Examples of processing levels:

- Low-level processing
  - image manipulation  $\Rightarrow$  *resizing, color adjustments, filtering, etc.*
  - feature extraction  $\Rightarrow$  *edges, gradients, etc.*
- Mid-level processing
  - panorama stitching
  - Structure from Motion (SfM)  $\Rightarrow$  2D to 3D
  - Optical Flow  $\Rightarrow$  velocities
- High-level processing
  - classification  $\Rightarrow$  *what is in the image?*
  - detection  $\Rightarrow$  *where are they?*
  - segmentation (semantic or instance)  $\Rightarrow$  *segment image and give names*

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hue x5  
→



filter (high pass)  
→



## Examples of processing levels:

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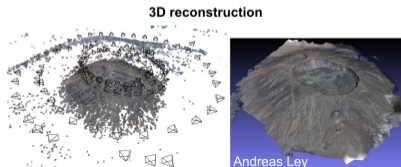
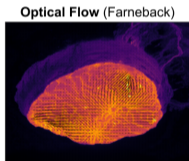
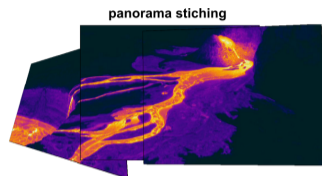
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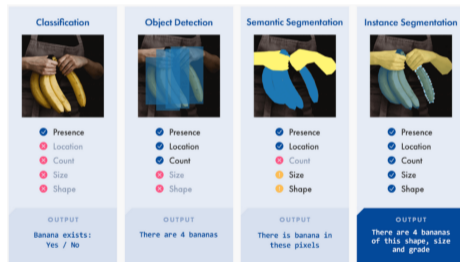
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Credit: cloudfactory

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1. Motivation

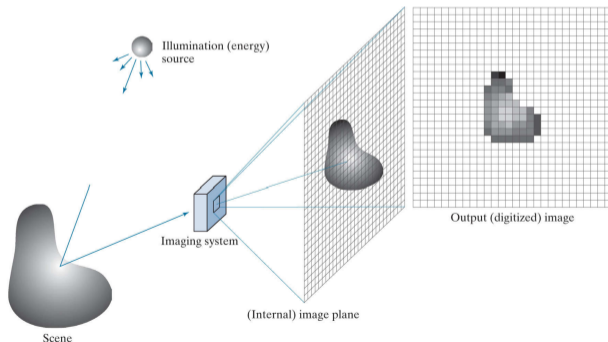
2. What is a digital image?

1. image acquisition
2. sampling and quantization
3. 3D projection on 2D plane
4. color image
5. color spaces
6. image histogram

3. Point operations

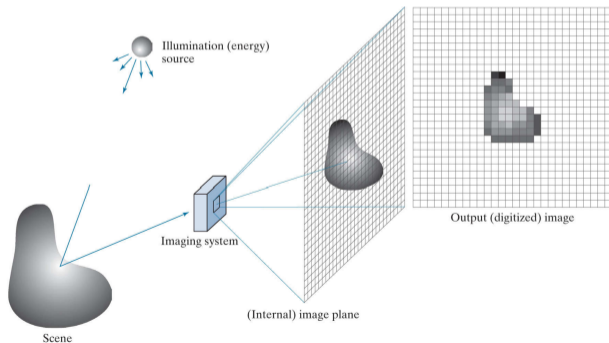
4. Image manipulation with Python

1. energy from an **illumination source** is reflected from a **scene**
2. the **imaging system** collects the incoming energy and focuses it onto an **image plane**  
NB: light-sensing instruments typically use 2-D arrays of photosensors to record incoming light intensity  
 $I(x)$ : the CCD (Charge-Coupled Device)
3. the image plane is sampled and quantized to produce a **digital image**

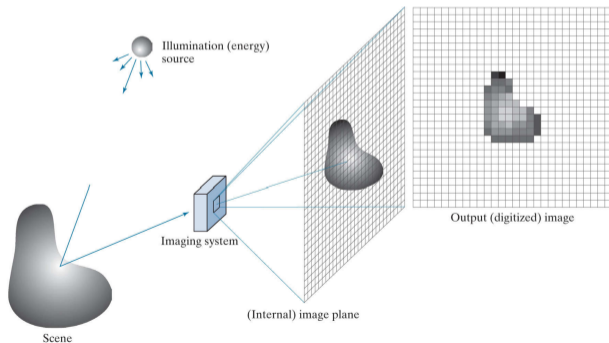


## 2.1. image acquisition

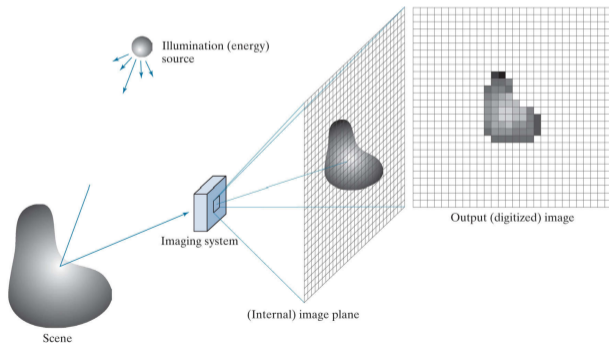
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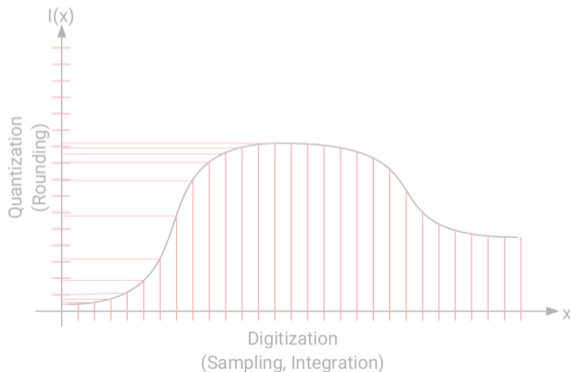
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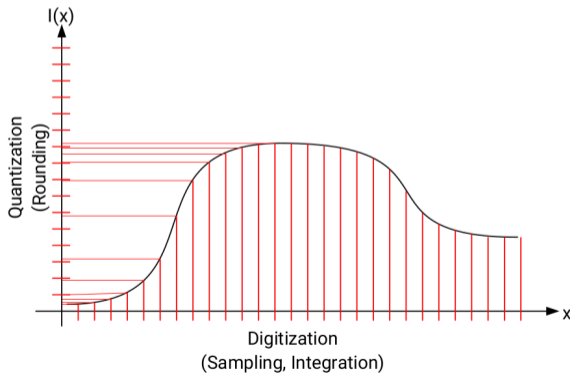


- each photosensor records incident light
- digitalization of an analog signal involves two operations
  - spatial sampling (= discretization of space domain)
  - intensity quantization (= discretization of incoming light signal)





- each photosensor records incident light
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  - **spatial sampling** (= discretization of space domain)
  - **intensity quantization** (= discretization of incoming light signal)



## spatial sampling (= discretization of space domain)

⇒ smallest element resulting from the discretization of the space is called a pixel (=picture element)

(512, 512)



(128, 128)



(64, 64)



(32, 32)



## intensity quantization (= discretization of light intensity signal)

⇒ typically, 256 levels (8 bits/pixel =  $2^8$  values) suffices to represent the intensity

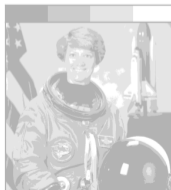
8-bit resolution  
 $2^8 = 256$  gray levels



3-bit resolution  
 $2^3 = 8$  gray levels



2-bit resolution  
 $2^2 = 4$  gray levels



1-bit resolution  
 $2^1 = 2$  gray levels



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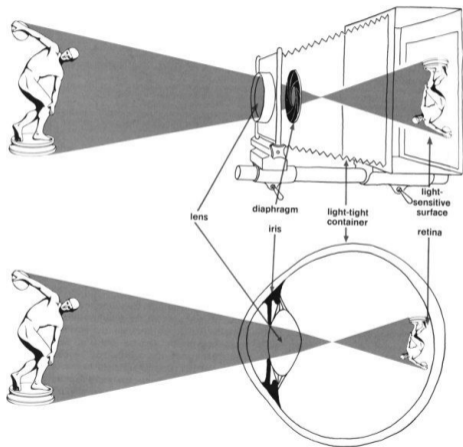


1-bit resolution  
 $2^1 = 2$  gray levels



But how is the 3D world projected on a 2D plane?

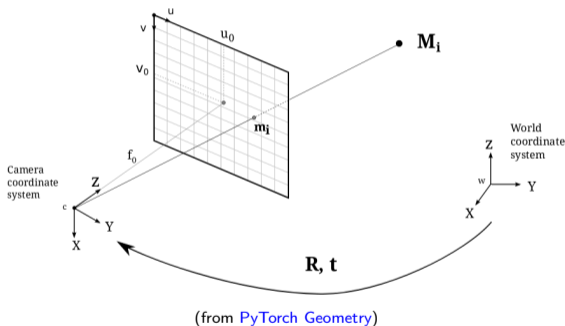
⇒ comparison between human eye and pinhole camera:



*In 1514, Leonardo da Vinci explained: "By letting the images of illuminated objects penetrate through a small hole into a very dark room, you will then intercept these images on a white sheet of paper placed in this room. [...] but they will be smaller and reversed".*

Image = 3D world projection on 2D

⇒ projection using the **pinhole camera model**:



Perspective transformation:

$$s \, m' = K[R|t]M' \quad (1)$$

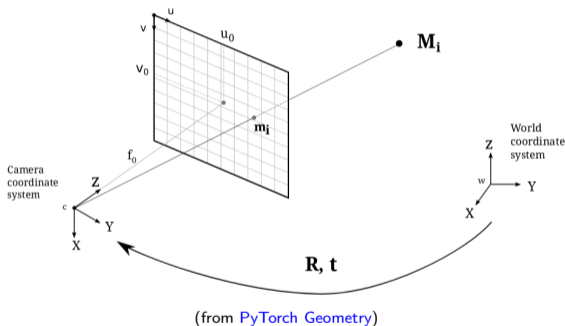
$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} \quad (2)$$

where:

- $M'$  = 3D point in space with coordinates  $[X, Y, Z]^T$  expressed in Euclidean coordinates
- $m'$  = projection of the 3D point  $M'$  onto the image plane with coordinates  $[u, v]^T$  expressed in pixel units
- $K$  = camera calibration matrix (a.k.a. intrinsics parameters matrix)
  - $f_x, f_y$  = focal lengths expressed in pixel units
  - $u_0, v_0$  = coordinates of the optical center (aka principal point), origin in the image plane
- $[R|t]$  = joint rotation-translation matrix (a.k.a. extrinsics parameters matrix), describing the camera pose, and translating from world coordinates to camera coordinates

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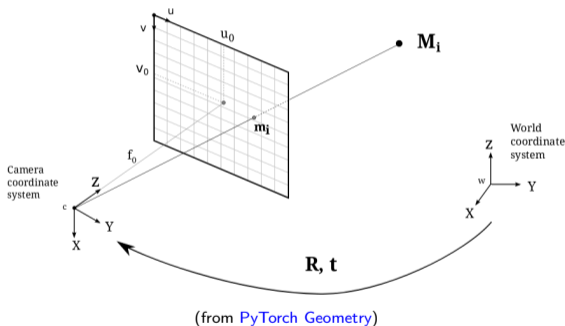
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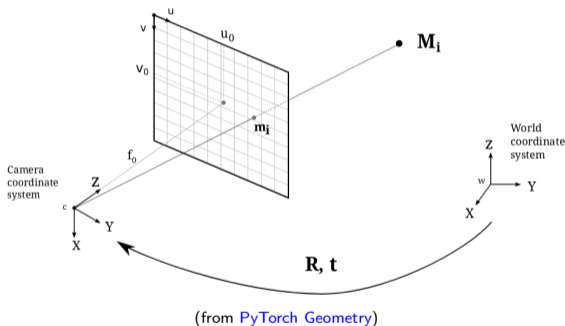
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$$s \, m' = K[R|t]M' \quad (1)$$

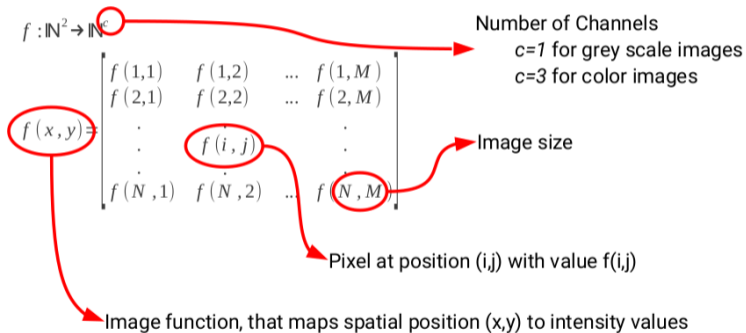
$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} \quad (2)$$

where:

- $M'$  = 3D point in space with coordinates  $[X, Y, Z]^T$  expressed in Euclidean coordinates
- $m'$  = projection of the 3D point  $M'$  onto the image plane with coordinates  $[u, v]^T$  expressed in pixel units
- $K$  = camera calibration matrix (a.k.a. intrinsics parameters matrix)
  - $f_x, f_y$  = focal lengths expressed in pixel units
  - $u_0, v_0$  = coordinates of the optical center (aka principal point), origin in the image plane
- $[R|t]$  = joint rotation-translation matrix (a.k.a. extrinsics parameters matrix), describing the camera pose, and translating from world coordinates to camera coordinates



⇒ digital image function  $f(x, y)$



⇒ digital image function  $f(x, y)$

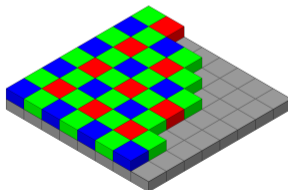
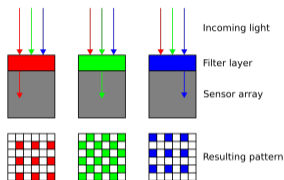
	columns									
	0	1	2	3	4	5	6	7	8	9
0	24	24	67	103	87	79	176	138	94	180
1	98	53	66	226	34	34	241	240	24	143
2	228	107	60	58	144	251	137	93	86	130
3	155	108	132	159	129	141	245	211	100	255
4	91	187	67	135	49	175	193	61	13	183
5	199	251	80	255	121	105	222	147	226	63
6	181	27	56	238	113	158	176	47	167	109
7	38	172	18	192	184	162	181	202	17	72
8	13	106	30	17	53	68	178	232	91	219
9	211	181	78	255	13	185	204	106	131	70

Typical ranges:

- `uint8` = [0-255] (0=black, 255=white)  
(8 bits = 1 byte =  $2^8 = 256$  values per pixel)
- `float32` = [0-1] (0=black, 1=white)  
(32 bits = 4 bytes =  $4.3e9$  values per pixel)

How do we record colors?

⇒ **Bayer Filter**: color filter array for arranging RGB color filters on a square grid of photosensors

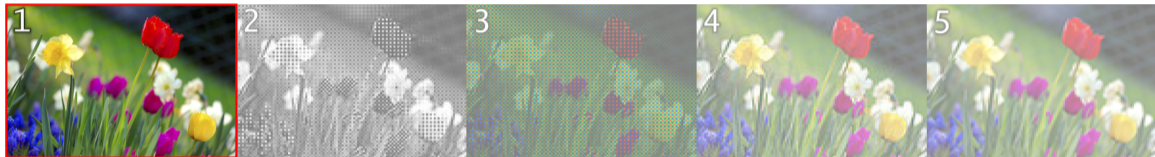


(source [wikipedia](#))

***NB:** notice the filter pattern is 1/2 green, 1/4 red and 1/4 blue ⇒ more green photosensors are used in order to mimic the physiology of the human eye, which is more sensitive to green light.*

How do we record colors?

⇒ **Bayer Filter**: color filter array for arranging RGB color filters on a square grid of photosensors



1. Original scene

2. Output of a  $120 \times 80$ -pixel sensor with a Bayer filter

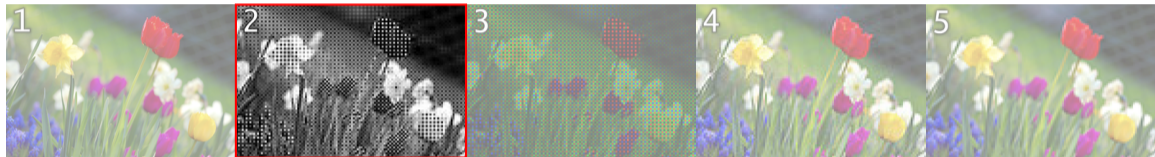
3. Output color-coded with Bayer filter colors

4. Reconstructed image after interpolating missing color information (a.k.a. demosaicing)

5. Full RGB version at  $120 \times 80$ -pixels for comparison

How do we record colors?

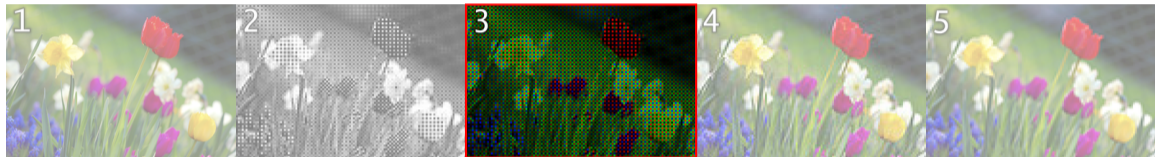
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How do we record colors?

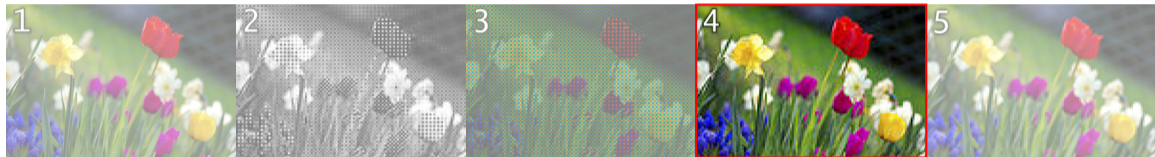
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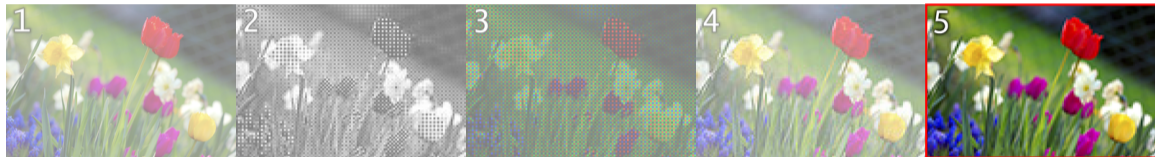
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How do we record colors?

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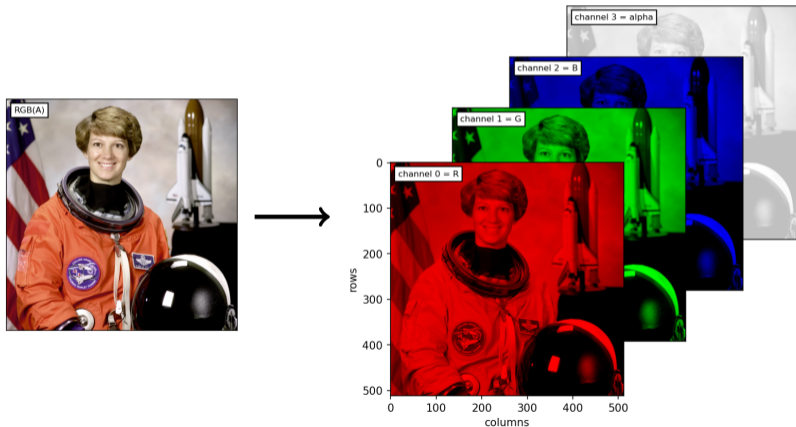


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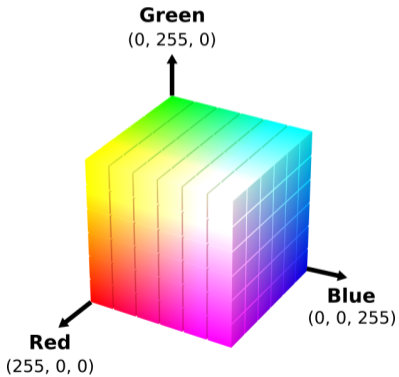
⇒ color image = 3D tensor in colorspace

- **RGB** = Red + Green + Blue bands (.JPEG)
- **RGBA** = Red + Green + Blue + Alpha bands (.PNG, .GIF, .BMP, TIFF, .JPEG 2000)

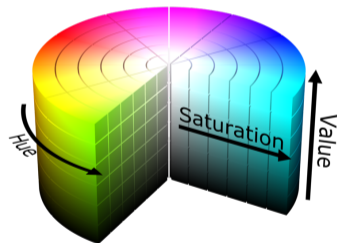


Other ways to represent the color information?

### RGB colorspace



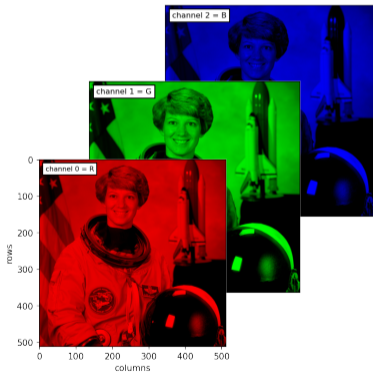
### HSV colorspace



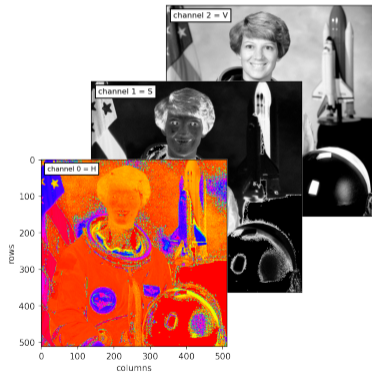
- Hue (H) = [0-360]  $\Rightarrow$  shift color
- Saturation (S) = [0-1]  $\Rightarrow$  shift intensity
- Value (V) = [0-1]  $\Rightarrow$  shift brightness

3D tensor with different information:

### RGB colorspace



### HSV colorspace



## HSV allows for more intuitive color adjustments:

- more saturation  $S$   
⇒ more intense colors



- more value  $V$   
⇒ brighter colors

- shift hue  $H$   
⇒ shift color

## HSV allows for more intuitive color adjustments:

- more saturation  $S$   
⇒ more intense colors



- more value  $V$   
⇒ brighter colors



- shift hue  $H$   
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## HSV allows for more intuitive color adjustments:

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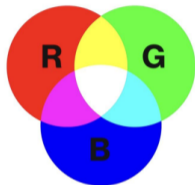
- shift hue  $H$   
⇒ shift color



## Additive vs. Subtractive Color Models:

### RGB (Additive Model)

- ⇒ used for devices that emit light (monitors, TVs, smartphones)
- ⇒ additive model: colors are created by combining different intensities of red, green, and blue light
  - combining all three colors at full intensity results in *white* light, absence of all results in *black*



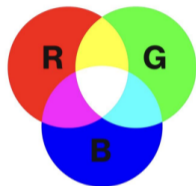
### CMYK (Subtractive Model)

- ⇒ used for printing on paper and other physical media
- ⇒ subtractive color model: colors are created by subtracting light reflected off the paper
  - combining all three colors ideally absorb all light, resulting in *black* (NB: in printers black ink is added to achieve deeper blacks and reduce usage of the other inks)

## Additive vs. Subtractive Color Models:

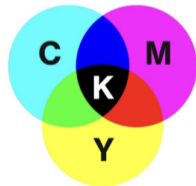
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### CMYK (Subtractive Model)

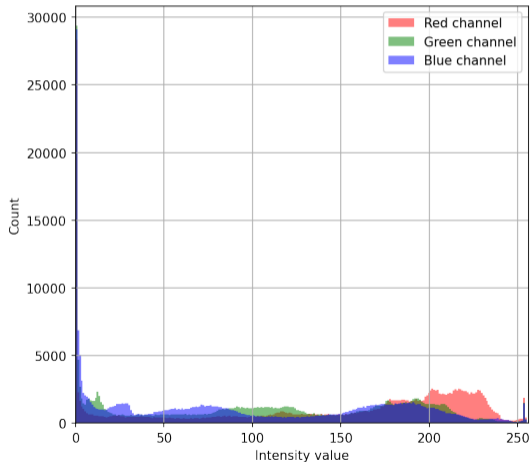
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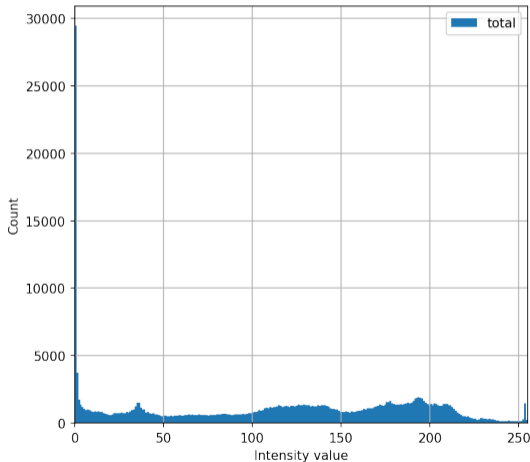
Histogram of pixel values in each band:

original (uint8)



Histogram of pixel values after conversion from RGB (3-bands) to gray-scale (1-band):

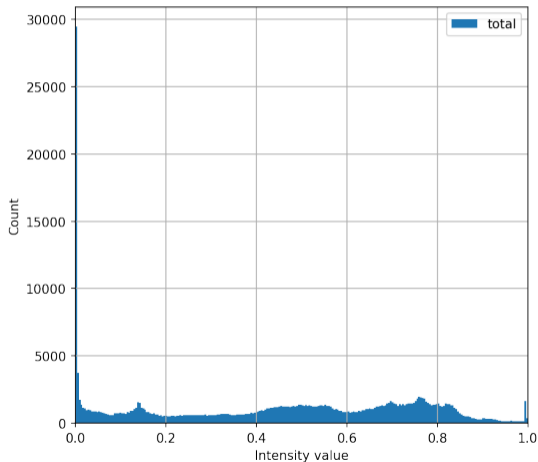
gray-scale (uint8)



***NB:** weights are chosen to mimic human perception of red, green and blue: the weight on the green band is larger because the human eye has greater sensitivity to green (the retina contains more photoreceptor cells (cones) that are tuned to detect green light)*

## Histogram of pixel values after conversion to float values (range [0-1])

gray-scale (float)



1. Motivation

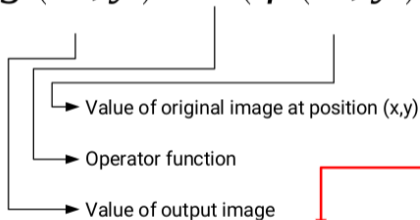
2. What is a digital image?

**3. Point operations**

1. homogeneous point operations
2. inhomogeneous Point Operations

4. Image manipulation with Python

$$g(x, y) = T(f(x, y), x, y)$$



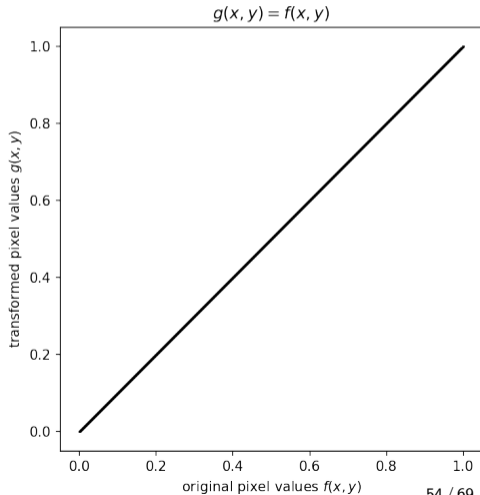
Inhomogeneous PO:  $T$  is dependent on  $(x, y)$

Homogeneous PO:  $T$  is NOT dependent on  $(x, y)$

## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

identity



## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

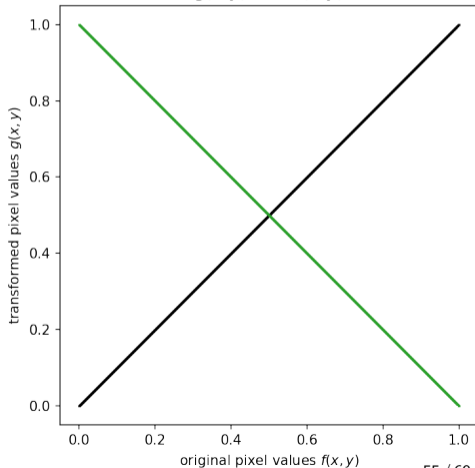
identity



inverse



$$g(x, y) = 1 - f(x, y)$$



## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

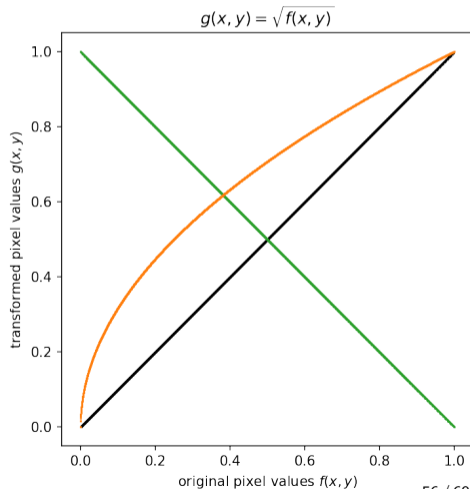
identity



inverse



square root





## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

identity



inverse



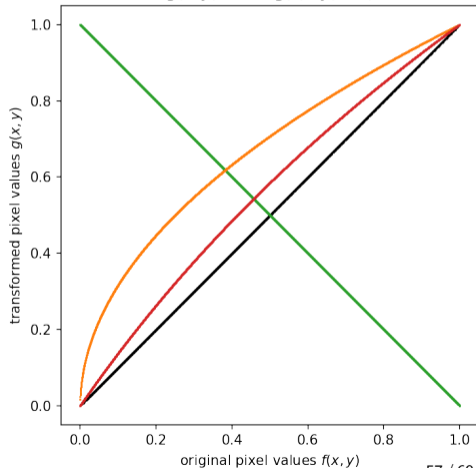
square root



logarithm



$$g(x, y) = a \cdot \log(f(x, y) + 1)$$



## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

identity



inverse



square root



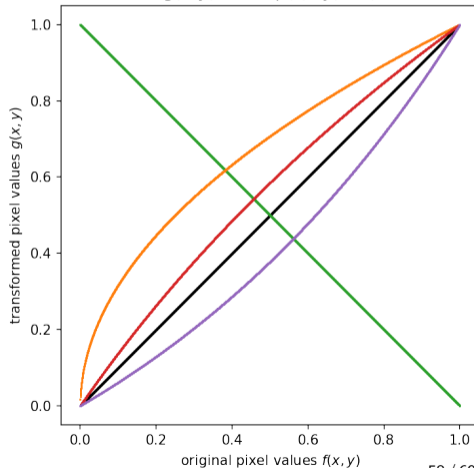
logarithm



exponential



$$g(x, y) = a \cdot \exp(f(x, y) - 1)$$



## Homogeneous Point Operations (does not depend on pixel position)

### 1. image intensity transformation using standard mathematical operations ( $\Rightarrow$ adjust pixel color 0=black / 1=white)

identity



inverse



square root



logarithm



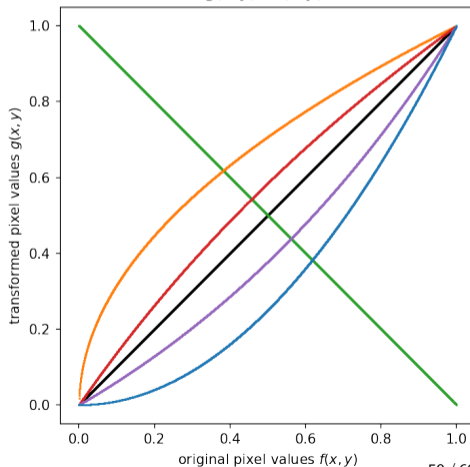
exponential



square

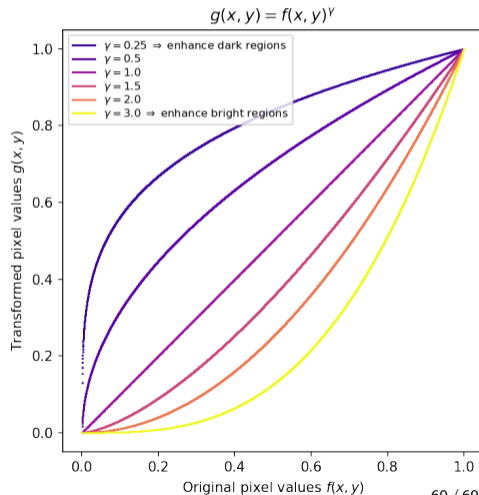
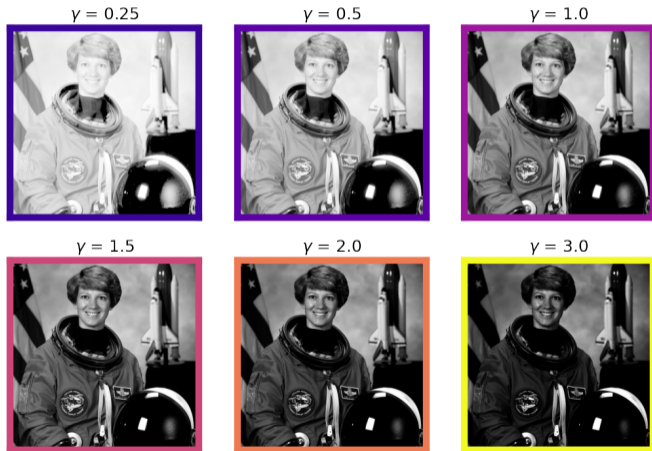


$$g(x, y) = f(x, y)^2$$



## Homogeneous Point Operations (does not depend on pixel position)

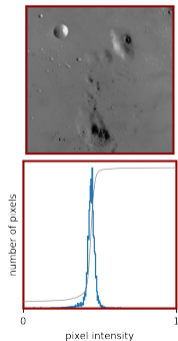
### 1. image intensity transformation using Gamma correction ( $\Rightarrow$ power-law transformation)



## Homogeneous Point Operations (does not depend on pixel position)

### 2. image contrast adjustment (⇒ adjust image histogram)

ORIGINAL image  
low contrast



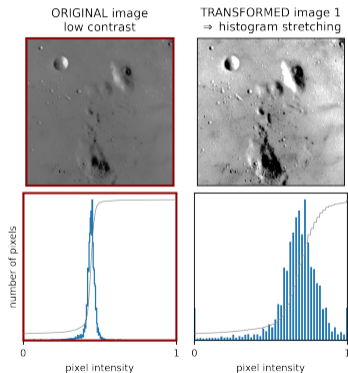
Modified after: [skimage-tutorial](#)

### Original image (no stretch)

- ⇒ image pixel intensity values are limited to a narrow range
- ⇒ without stretch only a small portion of the full range of possible display levels is used
- ⇒ results in a low contrast image

## Homogeneous Point Operations (does not depend on pixel position)

### 2. image contrast adjustment (⇒ adjust image histogram)



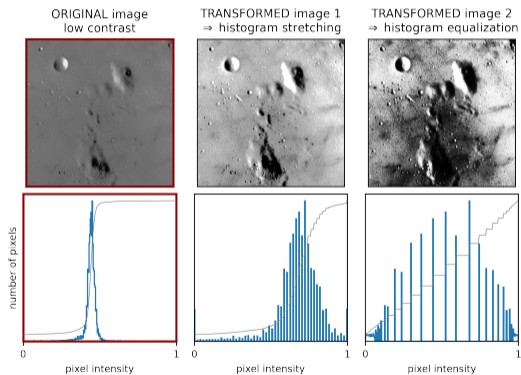
Modified after: [skimage-tutorial](#)

### Transformed image #1: linear histogram stretching

- ⇒ expand range of pixel intensities to stretch across full range of possible values
- ⇒ rescale pixel values to a specific range  
*EX: rescale pixel intensities between 2nd and 98th percentiles to occupy full 0-1 range*

## Homogeneous Point Operations (does not depend on pixel position)

### 2. image contrast adjustment (⇒ adjust image histogram)



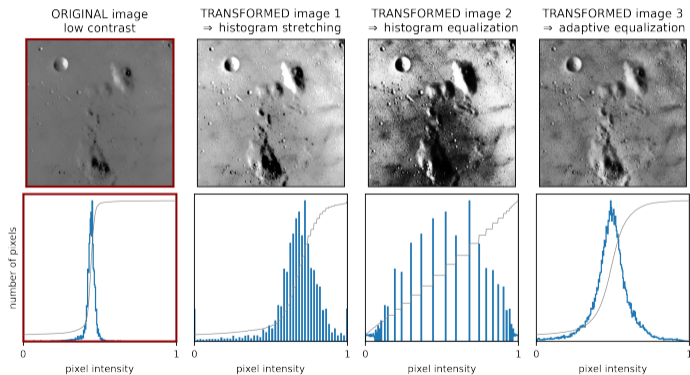
Modified after: [skimage-tutorial](#)

### Transformed image #2: histogram equalization

- ⇒ expand image pixel values on the basis of their frequency of occurrence (i.e. spreads out the most frequent intensity values)
- ⇒ equalized image has a roughly linear cumulative distribution function

## Homogeneous Point Operations (does not depend on pixel position)

### 2. image contrast adjustment (⇒ adjust image histogram)



### Transformed image #3: adaptive histogram equalization

- ⇒ algorithm "Contrast Limited Adaptive Histogram Equalization" (CLAHE)
- ⇒ computes histograms over different regions of the image for local contrast enhancement
- ⇒ local details can be enhanced even in regions that are darker or lighter than most of the image

Modified after: [skimage-tutorial](#)



## Inhomogeneous Point Operations (depends on pixel position)

EX: background detection / change detection


 $f_1$ 

 $f_i$ 

 $f_N$ 

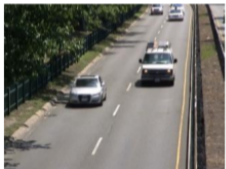
$$a(x, y) = \frac{1}{N} \sum_{i=0}^N f_i(x, y)$$

 $a(x, y)$ 

$$\begin{aligned} g_i(x, y) &= T(f(x, y), x, y) \\ &= f_i(x, y) - a(x, y) \end{aligned}$$



## Inhomogeneous Point Operations (depends on pixel position)



1. Motivation

2. What is a digital image?

3. Point operations

4. Image manipulation with Python

1. numpy tutorial

2. exercises

Numpy tutorial:

⇒ Open CV4GS\_02\_image-basics/[CV4GS\\_02\\_numpy-tutorial.ipynb](#)

Exercices:

⇒ Open `CV4GS_02_image-basics/CV4GS_02_exercices.ipynb`